

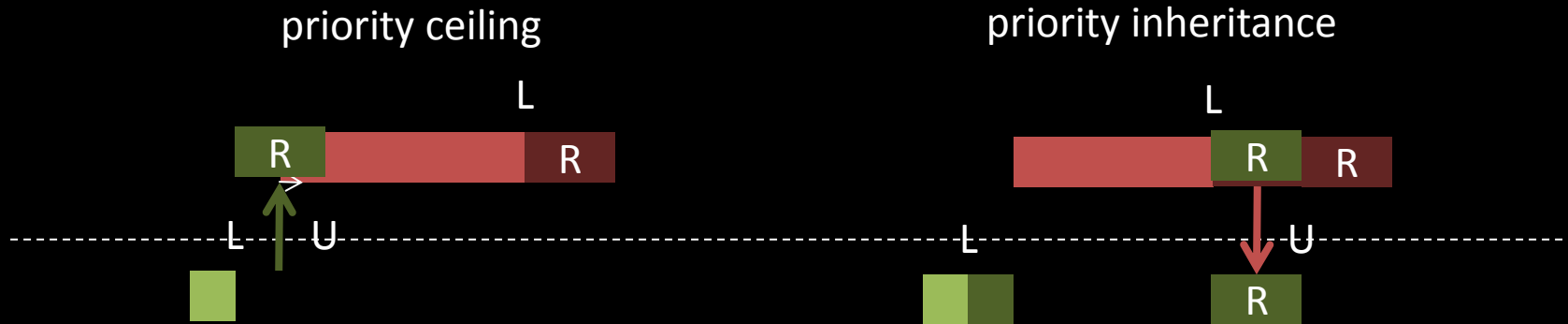
# Hard Real-Time Multiprocessor Scheduling

(Part II)

Marcus Völöp

two concepts to counteract priority inversion

- priority inheritance
- priority ceiling



# Locking Protocols

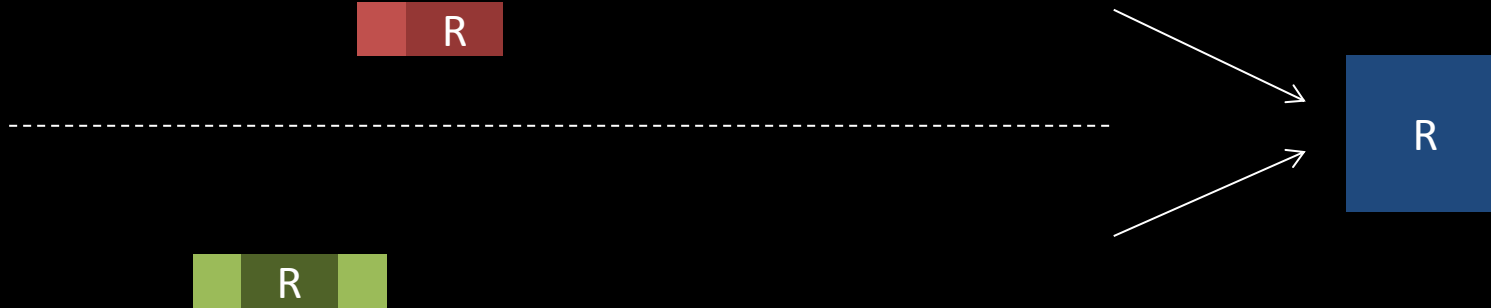
- Where to execute the critical section?  
local vs. remote
- How to order conflicting critical sections?  
FIFO vs. priorities
- How unrelated tasks affect the lock holders?
- Whether and how unrelated tasks are affected?

[Brandenburg '10,  
Brandenburg '13]

# Where to execute?

local vs. remote

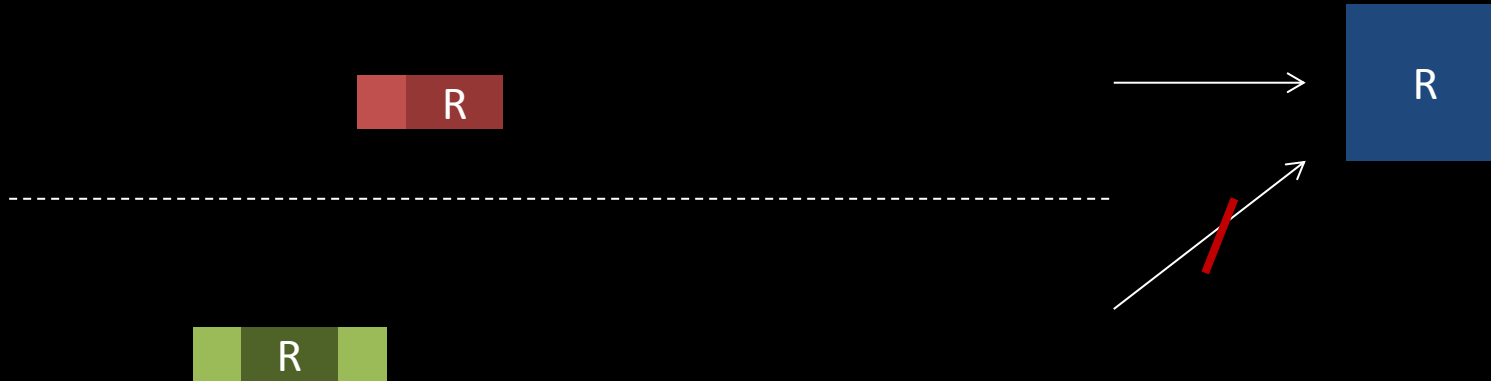
[Brandenburg '10,  
Brandenburg '13]



# Where to execute?

local vs. remote

[Brandenburg '10,  
Brandenburg '13]



# Where to execute?

local vs. remote

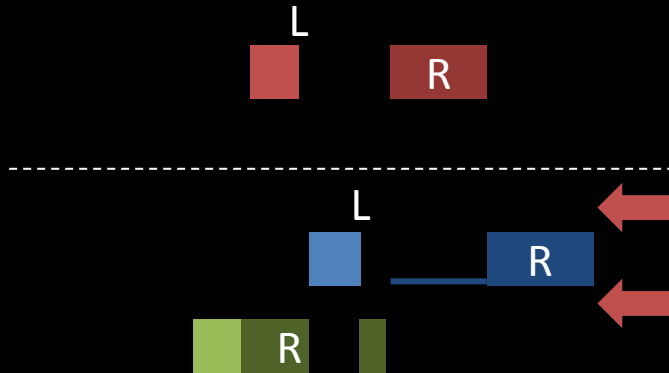
[Brandenburg '10,  
Brandenburg '13]



# How to order conflicts?

FIFO vs. priorities

[Brandenburg '10,  
Brandenburg '13]



FIFO:  $O(n)$

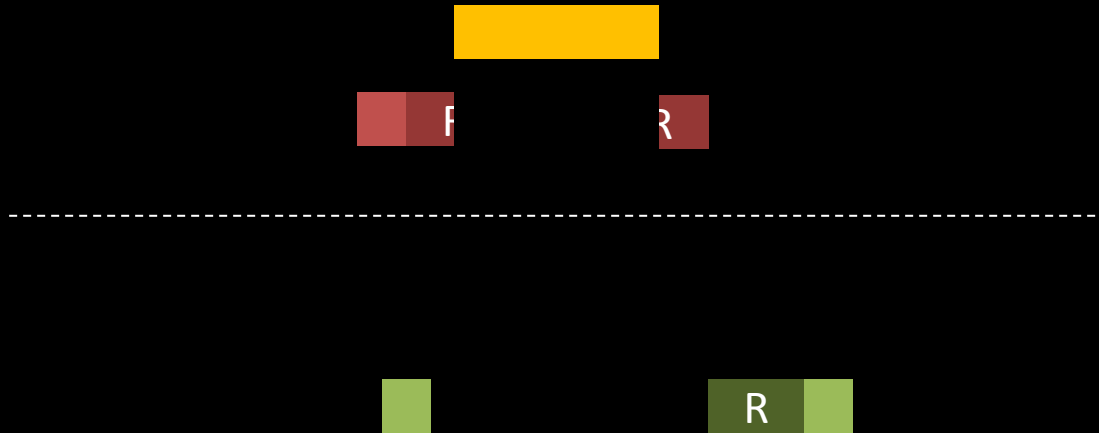
Priorities:  $O(\text{higher prioritized on other CPUs})$

$O(1)$  ?    $O(m)$  ?

# Unrelated tasks affect the lock

Block local vs. remote

[Brandenburg '10,  
Brandenburg '13]

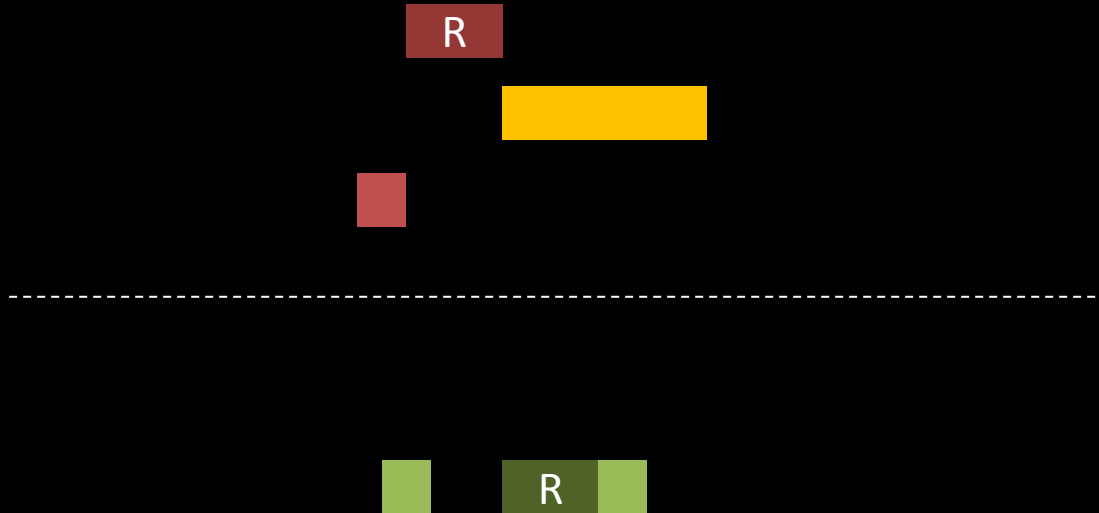


$$\sum_{\tau_j \in H(i)} c_j$$

# Unrelated tasks affect the lock

Block local vs. remote

[Brandenburg '10,  
Brandenburg '13]

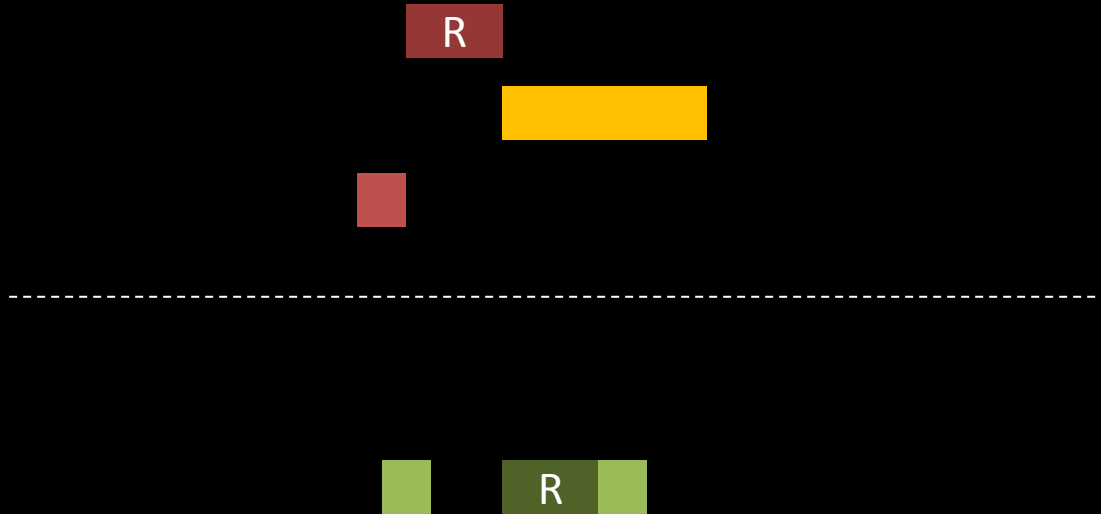


$$\sum_{\tau_j \in H(i)} c_j$$

# How unrelated threads are affected

Block local vs. remote

[Brandenburg '10,  
Brandenburg '13]

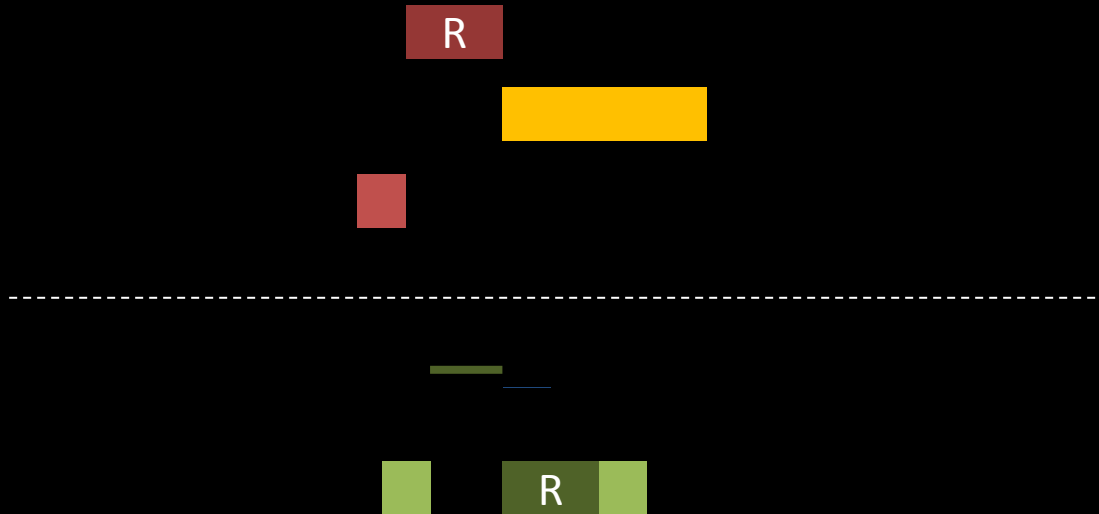


$$\sum_{\tau_j \in H(i)} c_j$$

# How unrelated threads are affected

Block local vs. remote

[Brandenburg '10,  
Brandenburg '13]



$$\sum_{\tau_j \in H(i)} c_j$$

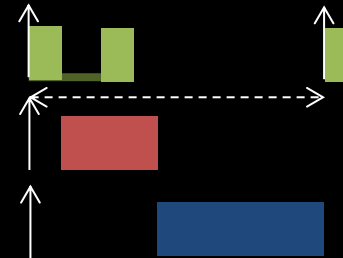
## schedulability analysis

- suspension-aware
- suspension-oblivious



## blocking

- priority-inversion blocking
- deferral blocking



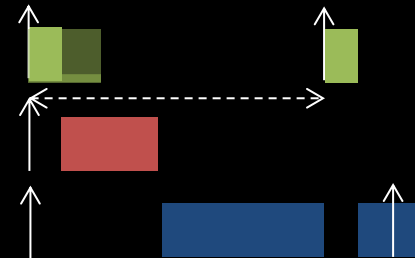
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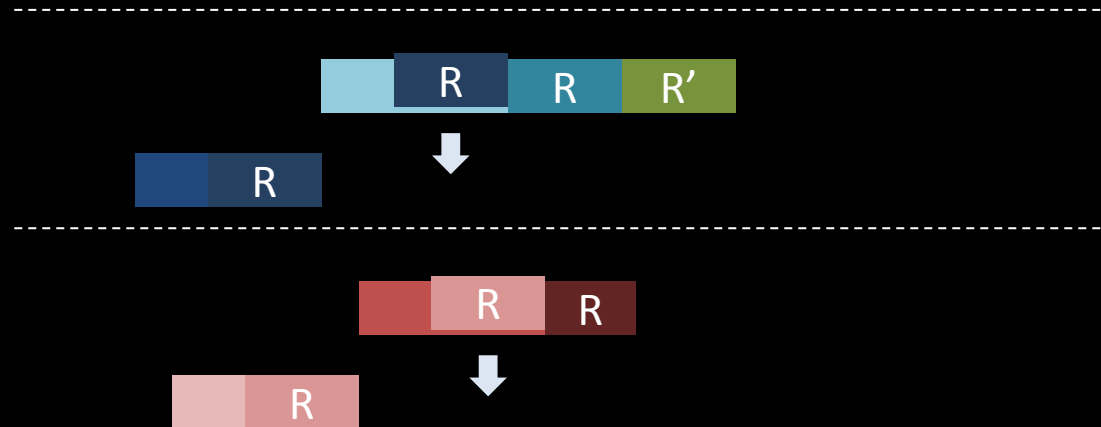
## blocking

- priority-inversion blocking
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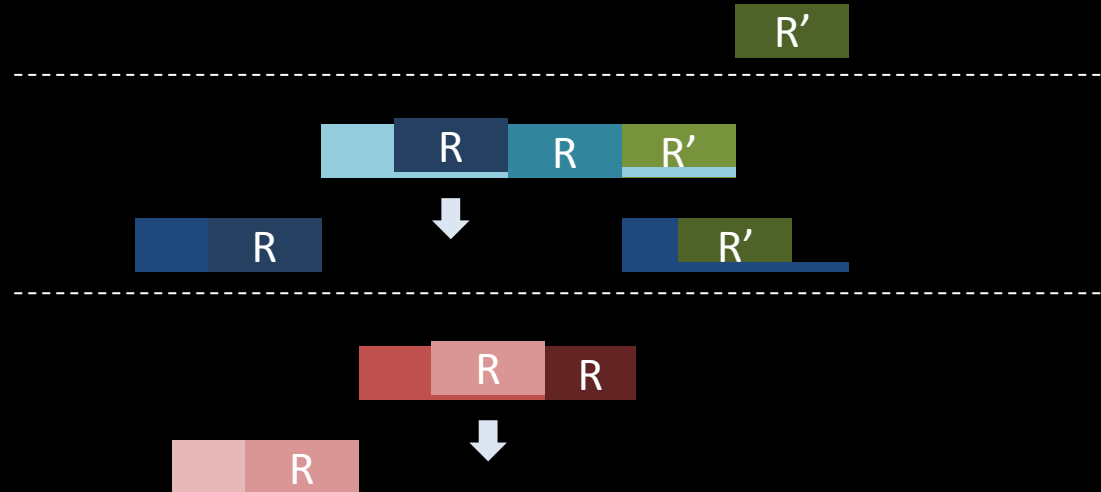
# Reuse UP Protocols?

Distributed Priority-Ceiling Protocol (DPCP) [Rajkuma, Sha, Lehocky '88]



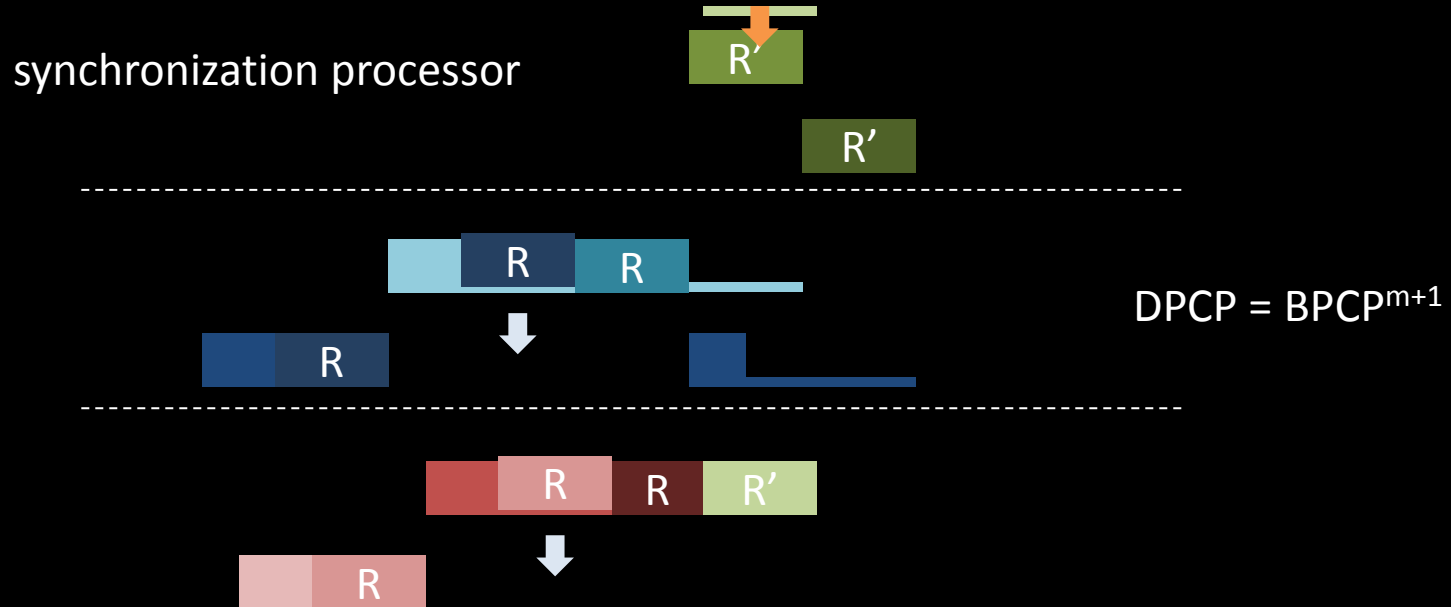
# Reuse UP Protocols?

Distributed Priority-Ceiling Protocol (DPCP) [Rajkuma, Sha, Lehocky '88]



# Reuse UP Protocols?

Distributed Priority-Ceiling Protocol (DPCP) [Rajkuma, Sha, Lehocky '88]



# Reuse UP Protocols?

## Multiprocessor Stack Resource Protocol (MSRP) [Gai, Lipari, Natale '01]

synchronization processor



$$\text{MSRP} = \text{MSRP}^{m+1}$$

Improved Analysis and Evaluation of Real-Time Semaphore Protocols for Partitioned Fixed Priority Scheduling '13

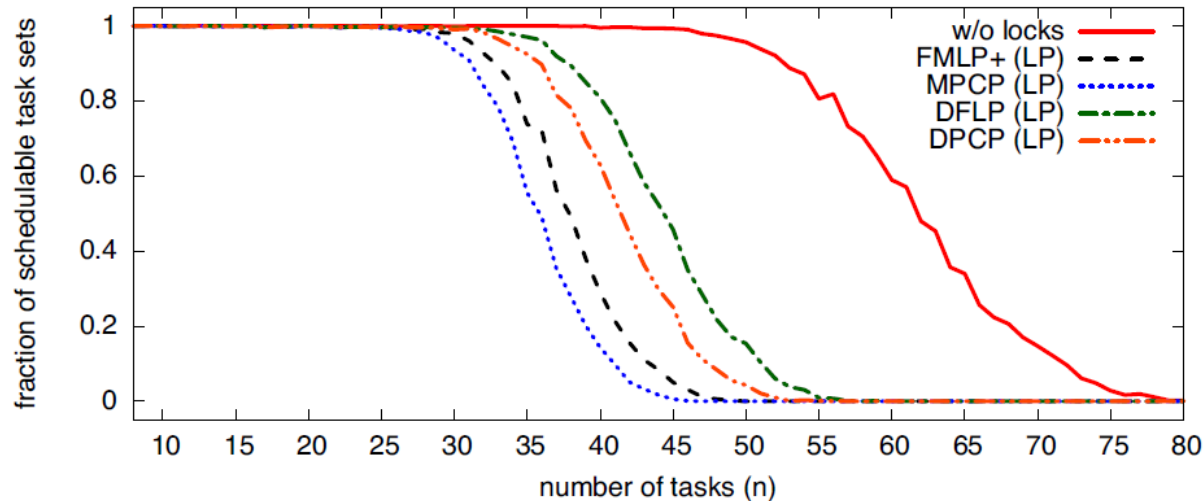
	MPCP [Rajkumar '90, Lakshmanan '09]	FMLP [Brandenburg '11]	DPCP [Rajkumar '88]	DFLP [Brandenburg '11]
wait queue	priority	FIFO	priority	FIFO
protocol type	shared mem. (local)	shared mem. (local)	distributed (sync. CPU)	distributed (sync. CPU)
asymptotically optimal (wrt. maximal blocking)	No	Yes	No	Yes



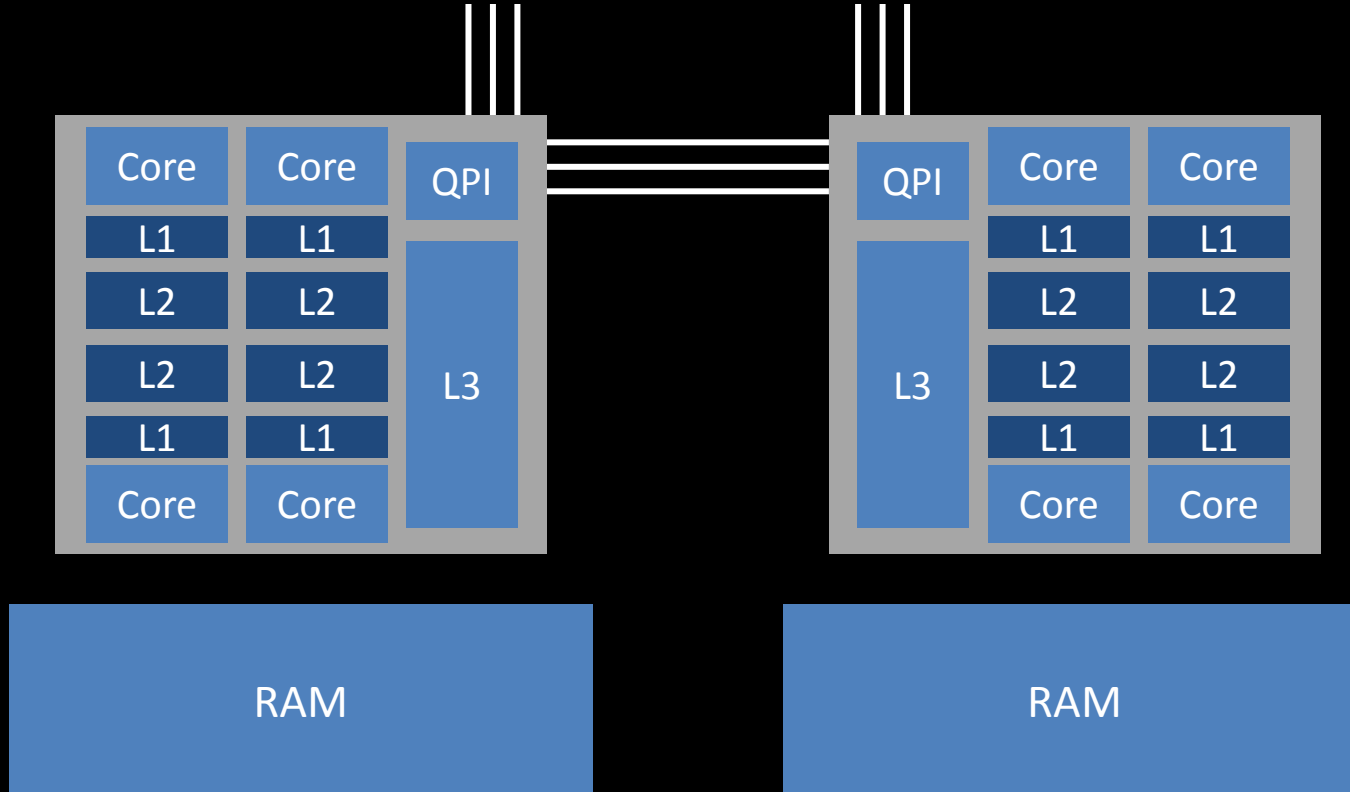
Improved Analysis and Evaluation of Real-Time Semaphore Protocols for Partitioned Fixed Priority Scheduling '13

## Overhead-Aware Schedulability

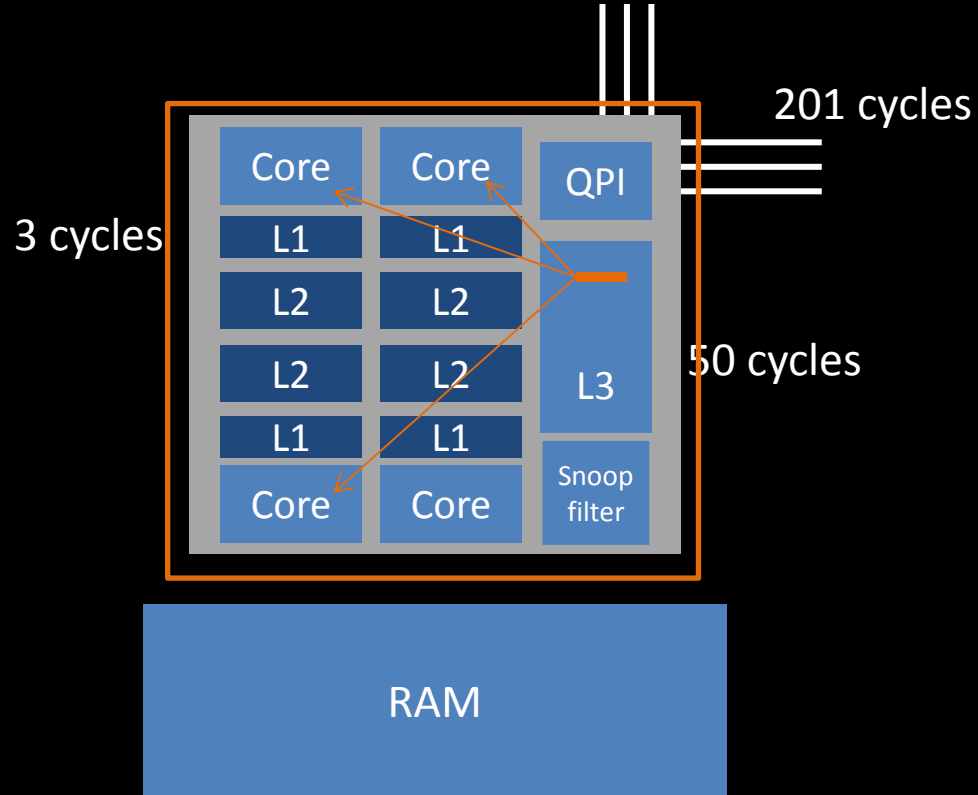
8 cores, 8 shared resources, max. 5 critical sections per task and resource,  $10\mu\text{s}$ - $50\mu\text{s}$  CS length, each task accesses a given resource with probability 0.3



# Caches



# Caches



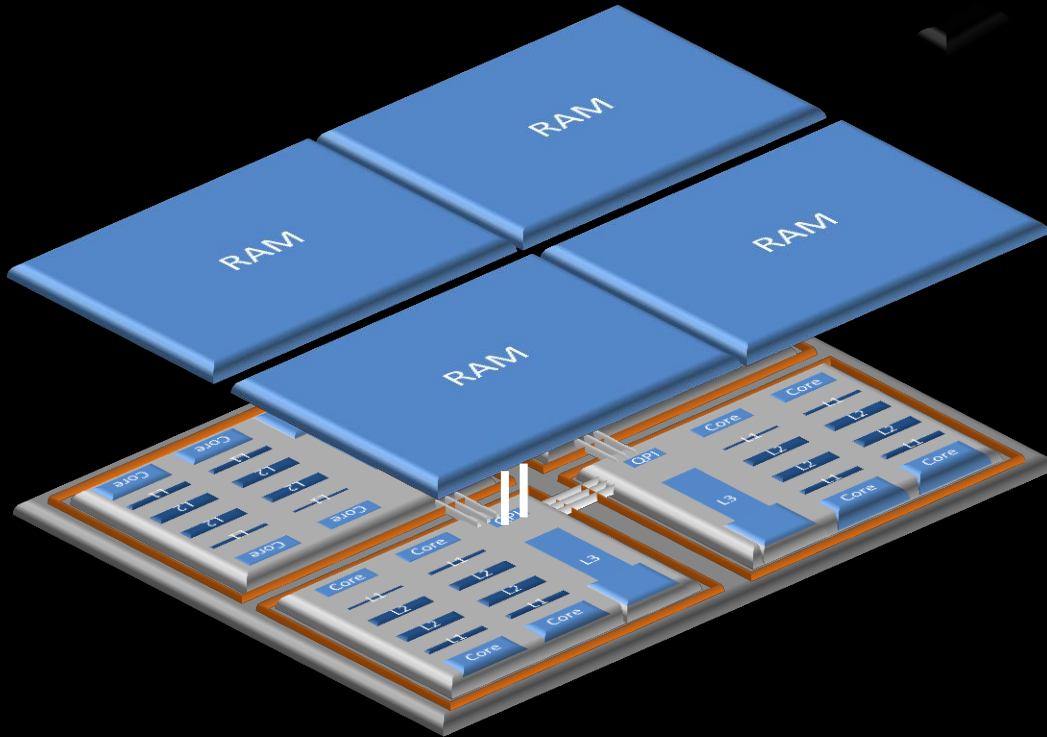
[Corey: OSDI '08]

reduce coherent traffic by  
keeping track of cached lines

- inclusive L3:  
line  $\in$  L1, L2  $\Rightarrow$  line  $\in$  L3
- snoop filter:  
keep address not data

# Caches

[Corey: OSDI '08]



reduce coherent traffic by  
keeping track of cached lines

- inclusive L3:  
 $\text{line} \in \text{L1, L2} \Rightarrow \text{line} \in \text{L3}$
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keep address not data

# RT - Locks for Clusters

Real-Time Resource-Sharing under Clustered Scheduling:  
Mutex, Reader-Writer, and k-Exclusion Locks  
Björn Brandenburg, Jim Anderson '11



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What if

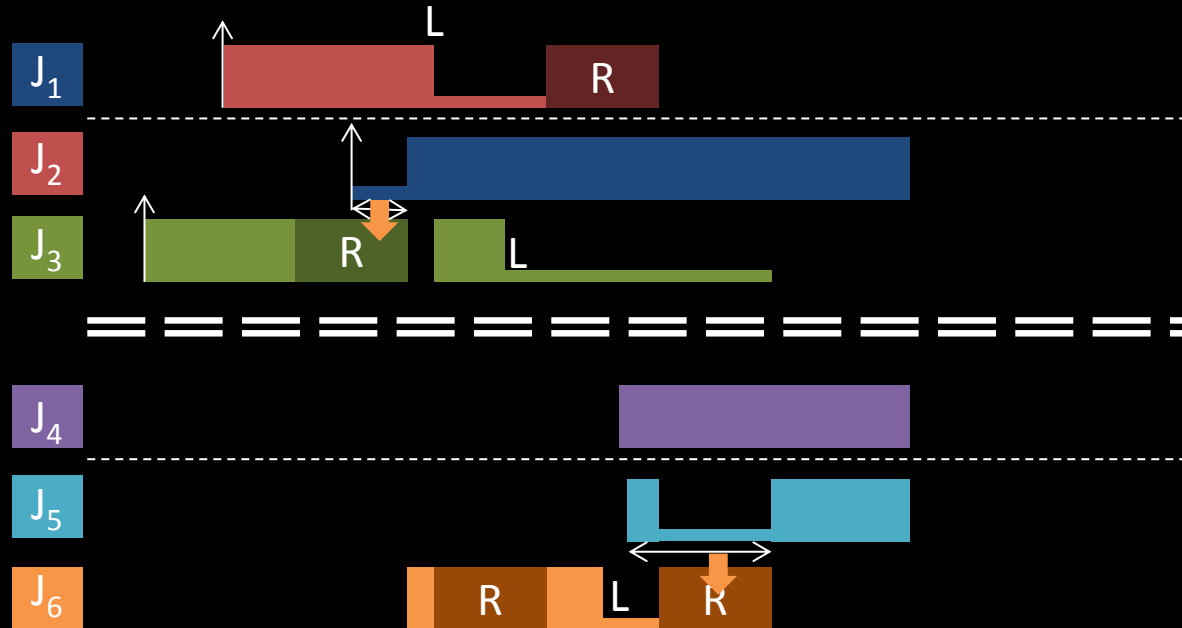
- every task helps out a little bit when it is released?
- only the n-highest prioritized tasks may acquire locks?

# RT - Locks for Clusters

Real-Time Resource-Sharing under Clustered Scheduling:

Mutex, Reader-Writer, and k-Exclusion Locks

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# RT - Locks for Clusters

Real-Time Resource-Sharing under Clustered Scheduling:

Mutex, Reader-Writer, and k-Exclusion Locks

Björn Brandenburg, Jim Anderson '11




- D1.  $J_i$  may issue a request only if it among the  $n = |\text{CPU}|$  highest prioritized jobs
- D2. When released at time  $t_a$ ,  $J_d$  becomes  $J_i$ 's priority donor if a)  $J_i$  was the  $c = |\text{Cluster}|$  highest-priority pending job released prior to  $J_d$ , b)  $J_d$  has one of the  $c$  highest base priorities, and c)  $J_i$  has issued a request that is incomplete
- D3.  $J_i$  inherits  $J_d$ 's priority
- D4. If  $J_d$  ceases to be among the  $c$  highest-priority jobs in its cluster, the newly released job takes over the donor role
- D5. / D6. schedule either  $J_i$  or its donor  $J_d$
- D7. a priority donor may not issue requests ( $J_d$  suspends in this case while being a priority donor)
- D8. If  $J_d$  finishes execution while being a donor,  $J_d$  remains the donor but is suspended
- D9.  $J_d$  stops being a donor if a)  $J_i$  completes its request, b)  $J_i$  becomes one of the  $c$  highest prioritized jobs c) another job takes over being the donor of  $J_i$

## Last Week:

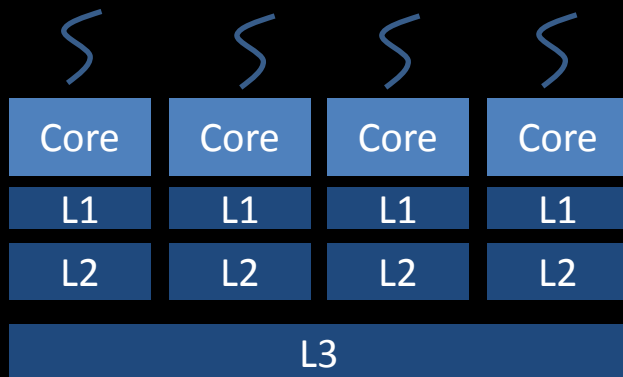
- Terminology and Notations
- Anomalies and Impossibility Results
- Partitioned Scheduling
- Global Scheduling
- Optimal MP Scheduling
- Practical Matters

## Today:

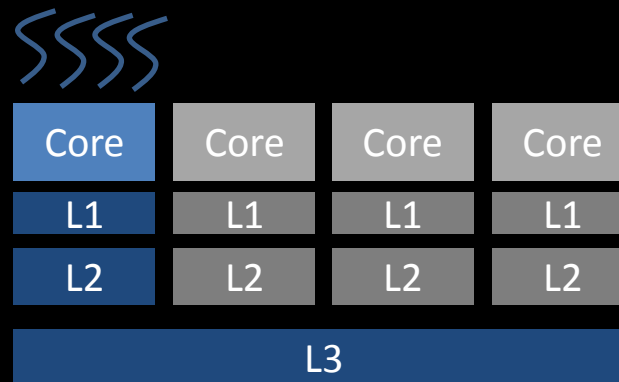
- Exercise:  
UP Resource Protocols
  - Resources
    - Caches / Memories
  - One More Resource
  - Dynamic Tasks
  - Peek and Poke into other  
Bleeding Edge Research
- 

## A Coordinated Approach for Practical OS-Level Cache Management in Multi-Core Real-Time Systems

Hyoseung Kim, Arvind Kandhalu, Ragunathan (Raj) Rajkumar (ECRTS '13)



40% slowdown



27% slowdown

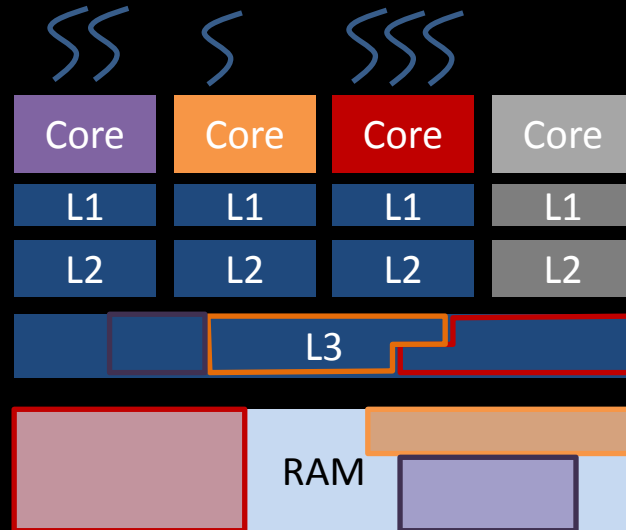
PARSEC on i7

## A Coordinated Approach for Practical OS-Level Cache Management in Multi-Core Real-Time Systems

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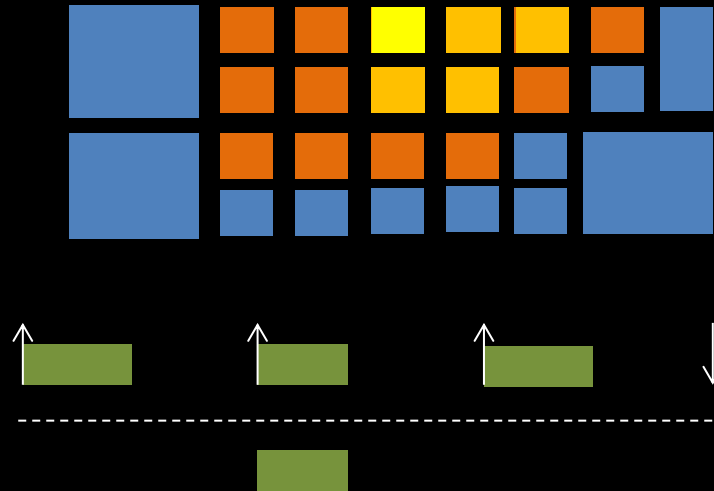
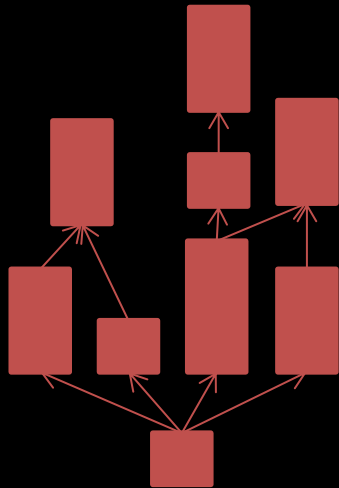


Algorithm and complexity for the global scheduling of sporadic tasks on multiprocessors with work-limited parallelism

S. Collette, L. Cucu, J. Goossens [Real-Time and Network Systems, '07]



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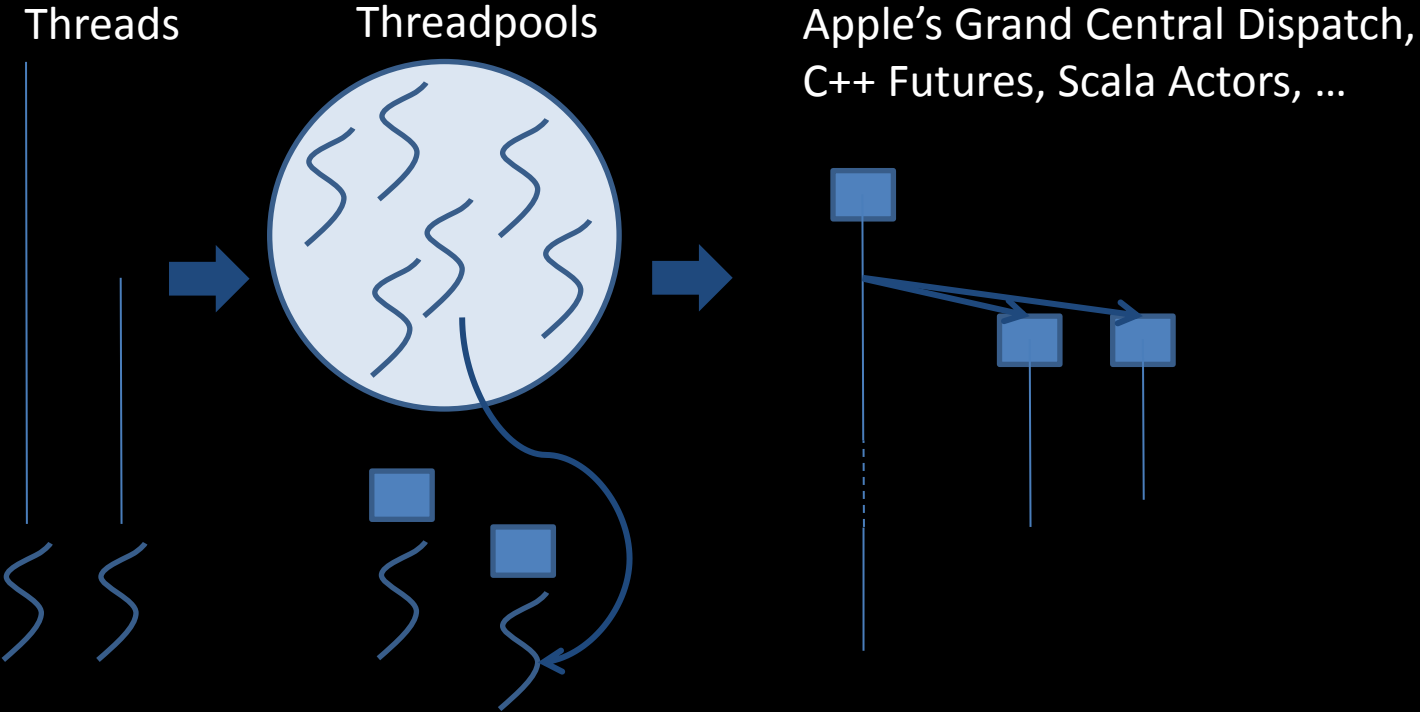


$$J_i \stackrel{\text{def}}{=} (C_i, P_i, \Gamma_i)$$

$$\Gamma_i \stackrel{\text{def}}{=} (\gamma_{i,1}, \gamma_{i,2}, \dots, \gamma_{i,m})$$

Job  $J_i$  with  $j$  CPUs  
completes in  $\gamma_{i,j} C_i$


# Dynamic Tasks / Runtime



## Last Week:

- Terminology and Notations
- Anomalies and Impossibility Results
- Partitioned Scheduling
- Global Scheduling
- Optimal MP Scheduling
- Practical Matters

## Today:

- Exercise:  
UP Resource Protocols
  - Resources
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  - One More Resource
  - Dynamic Tasks
  - Peek and Poke into other Bleeding Edge Research
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